

**BACHELOR OF SCIENCE (CBCS-2018 COURSE)**  
**F. Y. B. Sc. Sem-II : WINTER- 2022**  
**SUBJECT : STATISTICS : DISCRETE PROBABILITY & PROBABILITY**  
**DISTRIBUTIONS-II**

Day : Wednesday

Time : 02:00 PM-05:00 PM

Date : 21-12-2022

**W-18338-2022**

Max. Marks : 60

**N.B.**

- 1) All questions are **COMPULSORY**.
- 2) Figures to the right indicate **FULL** marks.
- 3) Use of non-programmable calculator is allowed.

**Q.1** Attempt **ANY TWO** of the following: **(12)**

- a) Suppose  $x$  and  $y$  are two discrete r.v.s. then  
 $\text{var}(ax + by) = a^2 \text{var}(x) + b^2 \text{var}(y) + 2ab \text{cov}(x, y)$
- b) State and prove lack of memory property of geometric distribution.
- c) Suppose  $x_1, x_2, x_3$  are three discrete r.v.s. with means 10, 20 and 40 and s.d.s 2, 4 and 6 respectively. Further  $\rho(x_1, x_2) = \frac{1}{4} = \rho(x_1, x_3)$  and  $\rho(x_2, x_3) = \frac{1}{2}$ .  
 Find    **i)**  $E(4x_1 + 2x_2 - 3x_3)$     **ii)**  $\text{var}(3x_1 - 2x_2 + x_3)$   
           **iii)**  $\text{var}(x_3 - x_2 - x_1)$         **iv)**  $\text{cov}(2x_1 + 3, 4 - 3x_2)$   
           **v)**  $\rho(3x_2 - 3, x_3 + 1)$        **vi)**  $\rho(4 + x_2, 5 - 2x_3)$

**Q.2** Attempt **ANY TWO** of the following: **(12)**

- a) Derive M.G.F. of Poisson distribution and coefficient of Skewness and Kurtosis.
- b) Define  $(r,s)^{\text{th}}$  row moments  $(\mu'_{rs})$  of a discrete bivariate distribution of  $(x,y)$ .  
 Hence show  $\mu'_{10} = E(x)$      $\mu'_{01} = E(y)$ ,  $\mu'_{11} = E(xy)$
- c) Obtain mean and variance of geometric distribution.

**Q.3** Attempt **ANY TWO** of the following: **(12)**

- a) Let  $(x,y)$  be a discrete bivariate r.v. with the following p.m.f.

<b>y</b> <b>x</b>	<b>0</b>	<b>1</b>	<b>2</b>	<b>3</b>
0	k	3k	2k	4k
1	2k	6k	4k	8k
2	3k	9k	6k	12k

- i)** Find k    **ii)** Are  $x$  and  $y$  independent?    **iii)**  $P(x + y \leq 1)$   
**iv)**  $P(x^2 + y^2 \leq 4)$

P.T.O.

- b) For the following joint probability distribution of  $(x,y)$  compute  $\rho(x,y)$  the correlation coefficient between  $x$  &  $y$ .

$y$ $x$	<b>0</b>	<b>1</b>	<b>2</b>
<b>0</b>	1/4	0	1/4
<b>1</b>	1/8	1/8	1/4

- c) If  $x \rightarrow$  Poisson ( $m$ ) such that  $P(x=0) = \frac{1}{2}$ , find  $E(x)$  and  $var(x)$ .

**Q.4** Attempt **ANY THREE** of the following: (12)

- a) Find the recurrence relation between the probabilities of Poisson distribution. State its use.
- b) Following are the marginal p.m.f. of  $x$  and  $y$ .

$x$	1	2	3
$P(x)$	0.3	0.3	0.4

$y$	1	2	3
$P(y)$	0.1	0.6	0.3

Assuming  $x$  and  $y$  to be independent. Obtain the joint probability distribution of  $x$  and  $y$ .

- c) Prove that
- i)  $cov(ax, by) = ab \cdot cov(x, y)$
  - ii)  $cov(x+c, y+d) = cov(x, y)$
  - iii)  $cov(x, x) = var(x)$
- d) Let  $x \rightarrow$  poisson ( $m$ ) such that  $P(x=2) = \frac{3}{4} P(x=1)$ . Find  $P(x=0)$  and the most probable value of  $x$ .

**Q.5** Attempt **ANY THREE** of the following: (12)

- a) Show that all the cumulants of poisson distribution are equal to the parameter  $m$ .
- b) State four real life situations in which geometric distribution can be applied.
- c) Define conditional probability distribution of  $x$  given  $y = y_j$ .
- d) Suppose  $x$  and  $y$  are two discrete r.v.s with joint probability distribution  $\{(x_i, y_j, p_{ij}); I=1 \dots m; j=1 \dots n\}$ .
- e) Two beads are selected at random without replacement from a bowl containing 4 blue, 1 red and 2 black beads. Let  $x$  denote the number of red beads drawn.  $Y$  denote the number of black beads drawn:
- i) Find the joint p.m.f. of  $(x,y)$
  - ii) Obtain the marginal p.m.f.s of  $x$  and  $y$ .
  - iii) Calculate  $P(x < y)$
- f) Show that all the cumulants of poisson distribution are equal to the parameter  $m$ .