

BACHELOR OF SCIENCE (CBCS-2018 COURSE)
F. Y. B. Sc. Sem-II :SUMMER- 2022
SUBJECT : MATHEMATICS : INTEGRAL CALCULUS & DIFFERENTIAL
EQUATIONS

Day : Friday

Date : 15-07-2022

S-18335-2022

Time : 11:00 AM-02:00 PM

Max. Marks : 60

N.B.:

- 1) All questions are **COMPULSORY**.
- 2) Figures to the right indicate **FULL** marks.

Q.1 Attempt **ANY TWO** of the following: **[12]**

- a) Prove that : $\int \sec^n x dx = \frac{\sec^{n-2} x \cdot \tan x}{n-1} + \frac{n-2}{n-1} \int \sec^{n-2} x dx$, and hence evaluate $\int \sec^6 x dx$.
- b) Evaluate : $\int \frac{x^2-1}{x^4+1} dx$.
- c) Evaluate : $\int_1^2 \frac{4-x}{x(x^2-2x+2)} dx$.

Q.2 Attempt **ANY TWO** of the following: **[12]**

- a) Prove that the solution of the differential equation of the form $\frac{dy}{dx} + Py = Q$ where P and Q are functions of x alone is $ye^{\int P dx} = \int e^{\int P dx} \cdot Q dx + c$.
- b) Solve : $(x^2 - 4xy - 2y^2) dx + (y^2 - 4xy - 2x^2) dy = 0$.
- c) Find the orthogonal trajectories of the family of rectangular hyperbolas $xy = c^2$.

Q.3 Attempt **ANY TWO** of the following: **[12]**

- a) Evaluate the surface area of the solid generated by revolving the cycloid $x = a(\theta - \sin \theta)$, $y = a(1 - \cos \theta)$ about the line $y = 0$.
- b) Find the volume of the solid generated by revolving the area included between the curves $y^2 = x^3$ and $x^2 = y^3$ about x - axis.
- c) Solve : $\tan \frac{y}{x} - \frac{y}{x} \sec^2 \frac{y}{x} + \sec^2 \frac{y}{x} \frac{dy}{dx} = 0$.

P.T.O.

Q.4 Attempt **ANY THREE** of the following: [12]

a) Define homogeneous differential equation and explain the method of its solution.

b) Solve : $(x^2y - 2xy^2) dx - (x^3 - 3x^2y) dy = 0$.

c) Evaluate : $\int \frac{dx}{5 + 4 \sin x}$.

d) Evaluate : $\int \frac{1}{\sqrt{3x^2 - 4x + 1}} dx$.

Q.5 Attempt **ANY FOUR** of the following: [12]

a) Evaluate : $\int_0^{\pi/2} \cos^{11} x dx$.

b) Evaluate : $\int \sin^2 x \cos^4 x dx$.

c) Eliminate a and b from the following:

$$y = ae^{-2x} + be^{2x}$$

d) Determine order and degree of the differential equation

$$\sqrt{1-x^2} dy + \sqrt{1-y^2} dx = 0.$$

e) Define : i) Integrating factor
ii) Exact differential equation .

f) Find the length of the arc of the curve $y = \log \sec x$ from $x = 0$ to $x = \frac{\pi}{3}$.

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