

**B.TECH. SEM -VI (COMPUTER) 2014 COURSE (CBCS) :
WINTER - 2017**

SUBJECT: DESIGN AND ANALYSIS OF ALGORITHMS

Day : **Tuesday**
Date : **21/11/2017**

Time: **10.00 AM TO 01.00 PM**
Max. Marks. 60

W-2017-2194

N.B.:

- 1) All questions are **COMPULSORY**.
- 2) Figures to the right indicate **FULL** marks.
- 3) Use of non-programmable **CALCULATOR** is allowed.
- 4) Assume suitable data if **NECESSARY**.

Q.1 Prove that if $f(n)=a_m n^m+\dots+a_1n+a_0$ then $f(n)=O(n^m)$ **(10)**

OR

Write a recursive Algorithm for computing Ackermann's function $A(m,n)$

$$A(m,n)=\begin{cases} n+1 & \text{if } m=0 \\ A(m-1,1) & \text{if } n=0 \\ A(m-1,A(m,n-1)) & \text{otherwise} \end{cases}$$

Q.2 Prove that the binary tree of depth 'k' has exactly 2^k-1 nodes. What is such type of tree called? **(10)**

OR

For the following list of elements show the traces of successful search for $x=151$ and unsuccessful search for $x=-14$.

{-5, -6, 0, 7, 9, 23, 54, 82, 101, 112, 125, 131, 142, 151}

Q.3 Give the Strassen's matrix multiplication method to multiply two matrices. **(10)**

OR

Show how Quicksort, sorts the following sequences of keys 1, 1, 1, 1, 1, 1, 1 and 5, 5, 8, 3, 4, 3, 2.

Q.4 Consider the following instance of the Knapsack problem **(10)**
 $n=3, m=20, (p_1, p_2, p_3)=(25, 34, 15)$ and $(w_1, w_2, w_3)=(18, 15, 10)$. Find all the feasible solution and indicate the Optimal solution out of them.

OR

Describe the Tree Vertex Splitting Algorithm with suitable example.

Q.5 Consider an instance $n=6, m=30$ and $w[1:6]=\{5, 10, 12, 13, 15, 18\}$. Show the state - space tree using Sum of Subsets Algorithm. **(10)**

OR

Describe FIFO Branch and Bound Algorithm.

Q.6 Let $L=10, n=6$, and $(l_1, l_2, l_3, l_4, l_5, l_6) = (5, 6, 3, 1, 2, 4)$ show the packing of these objects using Bin Packing Algorithm. **(10)**

OR

Explain Clique Decision Problem(CDP)

* * *