

**F.Y.B.SC. SEM – II (CBCS - 2016 COURSE) : WINTER - 2017**

**SUBJECT : STATISTICS : DISCRETE PROBABILITY &  
PROBABILITY DISTRIBUTIONS – II**

Day : **Friday** Time : **03.00 PM TO 06.00 PM**  
Date : **03/11/2017** **W-2017-0563** Max. Marks : 60

**N.B.:**

- 1) All questions are **COMPULSORY**.
- 2) Figures to the right indicate **FULL** marks.
- 3) Use of statistical tables and **CALCULATOR** is allowed.

**Q.1 A)** Choose the correct alternative for: **[06]**

- i) If  $X \sim \text{Poisson}(m)$  then,
  - a) Mean = Variance
  - b) Mean > Variance
  - c) Mean < Variance
  - d) Mean = 2 Variance
- ii) The second central moment of Poisson distribution with mean 4 is \_\_\_\_\_.
  - a) 4
  - b) 12
  - c) 16
  - d) 64
- iii) If  $x$  = number of candidates required to interview for the post of an officer then  $x$  follows:
  - a) Binomial distribution
  - b) Poisson distribution
  - c) Bernoulli distribution
  - d) Geometric distribution
- iv) If  $\text{Cov}(X, Y) = -10$ , then  $\text{Cov}(3X + 2, 10 - 5Y)$  is \_\_\_\_\_.
  - a) -10
  - b) 10
  - c) 20
  - d) 150
- v) If  $(X, Y)$  is a discrete bivariate r.v. with joint p.m.f.
 
$$p(x, y) = \frac{k}{x+y}; \quad x=0, 1$$

$$y=1, 2$$
 The value of  $k$  is \_\_\_\_\_.
  - a)  $\frac{3}{7}$
  - b)  $\frac{7}{3}$
  - c) 1
  - d)  $\frac{2}{7}$
- vi) If  $X \sim \text{Geometric}(0.25)$  taking values 1, 2, ....., then mean is \_\_\_\_\_.
  - a) 0.5
  - b) 0.25
  - c) 4
  - d)  $\frac{1}{4}$

**B)** State whether the following statements are true or false: **[06]**

- i)  $\text{Var}(X - Y) = \text{Var}(X) - \text{Var}(Y) - 2 \text{Cov}(X, Y)$ .
- ii) Marginal probability distribution of  $X$  is a univariate probability distribution.
- iii) If  $X$  and  $Y$  are independent Poisson r.v.s then  $X - Y$  is also Poisson random variable.
- iv) Poisson distribution is symmetric.
- v) Geometric distribution is symmetric.
- vi) The joint distribution function of bivariate discrete r.v.s lies between 0 and 1.

**Q.2** Attempt **ANY THREE** of the following: **[12]**

- a) State and prove additive property of Poisson distribution.
- b) Let  $X$  and  $Y$  have joint probability distribution given by.

$(X, Y)$	(1, 1)	(1, 2)	(1, 3)	(2, 1)	(2, 2)	(2, 3)
$p(x, y)$	$\frac{2}{15}$	$\frac{4}{15}$	$\frac{3}{15}$	$\frac{1}{15}$	$\frac{1}{15}$	$\frac{4}{15}$

Find marginal probability distribution of  $X$  and  $Y$ .

**P.T.O.**

- c) For  $(X, Y)$  a bivariate discrete r.v.,  $\sigma_x^2 = 9$ ,  $\sigma_y^2 = 4$ ,  $Cov(X, Y) = 4$ .  
Find: **i)**  $Var(2X - 3Y)$       **ii)**  $\rho(X, Y)$ .
- d) State and prove lack of memory property of a geometric distribution.

**Q.3** Attempt **ANY FOUR** of the following:

- a) If  $X$  follows Poisson ( $m$ ) such that  $P(X = 1) = P(X = 2)$ , find the probability mass function of  $X$ .
- b) If the probability that a certain test yields positive reaction is equal to 0.4. What is probability that less than 3 negative reaction occur before the first positive one?
- c) State the properties of joint distribution function of a two dimensional discrete r.v.s.
- d) Let  $X$  and  $Y$  be two discrete r.v.s with  $\sigma_x^2 = 9$ ,  $\sigma_y^2 = 16$ ,  $Var(2X - Y) = 51$ . Find  $Cov(X, Y)$ .
- e) Prove that  $Cov(X, X + Y) = Var(X) + Cov(X, Y)$ .

**Q.4** Attempt **ANY TWO** of the following:

- a) State the probability mass function (p.m.f.) of Poisson distribution with parameter  $m$ . Give four real life examples where Poisson distribution is expected.
- b) The joint p.m.f. of  $(X, Y)$  is given below:

	Y	-1	0	1	2
X					
	-2	1/9	1/27	1/27	1/9
	1	2/9	0	1/9	1/9
	3	0	0	1/9	4/27

- Compute : **i)**  $P(X > 0)$       **ii)**  $P(X < 0, Y > 0)$       **iii)**  $P(X \text{ is odd})$ .
- c) Obtain conditional mean and variance of  $X$  given  $Y = -3$  for the following joint probability distribution.

	Y	1	2	-3
X				
	0	0.1	0.2	0.3
	1	0.1	0.1	0.2

**Q.5** Attempt **ANY TWO** of the following:

- a) Let  $X$  be a discrete random variable with p.m.f.  
 $P(x) = pq^x$        $x = 0, 1, 2, \dots, 0 < p < 1, q = 1 - p$   
 $= 0$       otherwise  
 Find  $E(X)$  and  $Var(X)$ .
- b) Suppose  $X_1, X_2, X_3$  are three independent discrete r.v.s. with means 10, 20, and 40 and s.d.s 2, 4 and 6 respectively.  
 Find : **i)**  $E(4X_1 + 3X_2 + X_3)$       **ii)**  $Var(3X_1 + 2X_2 - 4X_3)$ .
- c) Let  $X$  and  $Y$  be two discrete r.v.s having joint probability distribution:

	Y	-2	0	2
X				
	-1	0.1	0.2	0.1
	0	0.2	0.1	0.1
	1	0.1	0.1	0

- Find: **i)**  $P(X + Y \leq 1)$       **ii)**  $P(X = 0 | Y = 0)$       **iii)**  $F(0, 2)$ .

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