

**SUBJECT: LINEAR ALGEBRA AND RANDOM PROCESS**

Day: - Monday  
Date: 10/12/2018

**W-2018-3115**

Time: 11.00 AM TO 02.00 PM  
Max Marks. 60

**N.B. :**

- 1) All questions are **COMPULSORY**.
- 2) Answer to Section-I and Section-II should be written in **SEPARATE** answer book.
- 3) Use of Non-programmable **CALCULATOR** is allowed.
- 4) Figures to right indicate **FULL** Marks.
- 5) Assume suitable data wherever **NECESSARY**.

**SECTION-I**

**Q.1** Prove that set at all solution  $a, b, c$  of equation  $a+b+2c=0$  is a sub space of vector space  $V_3(R)$  **(10)**

**OR**

Let  $R$  be the field of real number and  $P_n$  be the set of all polynomials of degree at most  $n$  over the field  $R$ . Prove that  $P_n$  is the vector space over the field  $R$ .

**Q.2** Solve the following assignment problem **(10)**

Machine	Operations			
	I	II	III	IV
A	10	5	13	15
B	3	9	18	3
C	10	7	3	2
D	5	11	9	7

**OR**

Find the initial feasible solution to the following transportation problem by (VAM) methods.

		To			
		X	Y	Z	
From	I	1	2	3	50
	II	3	2	1	80
	III	4	5	6	75
	IV	3	1	2	95
		120	80	8	

**Q.3** Given  $\frac{dy}{dx} = x^2(1+y)$  &  $y(1) = 1, y(1.1) = 1.233, y(1.2) = 1.548, y(1.3) = 1.979$  **(10)**  
evaluate  $y(1.4)$  by Adams – Bash forth method

**OR**

Apply Runge-Kutta method to find an approximate value of  $y$  for  $x = 0.2$  in steps of 0.1, if  $dy/dx = x+y^2$ , given that  $y=1$ , where  $x=0$ .

P.T.O.

**SECTION-II**

- Q.4** Consider an experiment of drawing randomly three balls from an urn containing two red, three white, & four, blue balls. Let  $(x,y)$  be a bivariate r.v. where  $x$  &  $y$  denote respectively the number at red & white balls chosen . **(10)**
- a) Find the range at  $(x,y)$ .
  - b) Find the joint pmf's at  $(x,y)$
  - c) Find the marginal pmf's at  $x$ & $y$ .

**OR**

Define Random variables & distribution function and write down properties of marginal distribution function.

- Q.5** Briefly explain the important characteristics of queuing system **(10)**

**OR**

A Supermarket has two girls ringing up sales at the counters. If the service time for each customer exponential with mean 4 minutes, and if people arrive in a Poisson fashion at the rate at 10 an hour calculate the

- a) Probability of having to wait for service?
  - b) Expected percentage of idle time for each girl?
- Q.6** Explain Poisson Random process. **(10)**

**OR**

Explain power spectral density function for random process.

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