

B.Tech Sem – IV (2007 Course) (Civil Engg.) : WINTER - 2018

SUBJECT: ENGINEERING MATHEMATICS – III

Day: Tuesday
Date: 13/11/2018

W-2018-2743

Time: 02.30 PM TO 05.30 PM
Max. Marks: 80

N.B.:

- 1) **Q. No. 1 and Q. No. 5 are COMPULSORY.** Out of the remaining attempt **ANY TWO** questions from Section – I and Section – II.
- 2) Figures to the right indicate **FULL** marks.
- 3) Answers to both the sections should be written in **SEPARATE** answer books.
- 4) Use of non programmable **calculator** is **ALLOWED**.
- 5) Draw neat and labeled diagrams **WHEREVER** necessary.
- 6) Assume suitable data, if necessary.

SECTION - I

Q.1 a) Solve by method of variation of parameters: $(D^2 - 1)y = e^{-x} \sin e^{-x} + \cos e^{-x}$ **(05)**

b) Solve: $\frac{dx}{2x} = \frac{dy}{-y} = \frac{dz}{4xy^2 - 2z}$ **(04)**

c) Apply factorization method to solve the equations (LU-decomposition Method) **(05)**

$$3x + 2y + 7z = 4$$

$$2x + 3y + z = 5$$

$$3x + 4y + z = 7$$

Q.2 Solve any three of the following: **(13)**

i) $(D^2 - 4)y = x \sinh x$

ii) $(D^2 - 2D + 1)y = xe^x \sin x$

iii) $(D^2 + 3D + 2)y = e^{e^x}$

iv) $x^2 \frac{d^2 y}{dx^2} - x \frac{dy}{dx} + y = \log x$

v) $(2x - 1)^2 \frac{d^2 y}{dx^2} + (2x - 1) \frac{dy}{dx} - 2y = 8x^2 - 2x + 3$

Q.3 a) The whirling speed of a shaft of length l is given by $\frac{d^4 y}{dx^4} - m^4 y = 0$ where **(06)**

$$m^4 = \frac{W \omega^2}{gEI}$$

and y is the displacement at distance x from one end. If the ends

of the shafts are constrained in long bearings, show that the shaft will whirl when $\cos ml \cosh ml = 1$

b) A tightly stretched flexible string has its ends fixed at $x = 0$ and $x = l$. At time $t = 0$, the string is given a shape defined by $F(x) = \mu x(l - x)$, where μ is constant, and then released. Find the displacement of any point x of the string at any time $t > 0$. **(07)**

P.T.O.

Q.4 a) Apply Runge Kutta method to find an approximate value of y for $x = 0.2$ in (07)
 steps of 0.1, if $\frac{dy}{dx} = x + y^2$, given that $y = 1$, where $x = 0$

b) Apply Gauss seidel iteration method to solve the equations (06)
 $20x + y - 2z = 17$
 $3x + 20y - z = -18$
 $2x - 3y + 20z = 25$

SECTION - II

Q.5 a) A problem in mechanics is given to the three students A, B and C whose (04)
 chances of solving it are $\frac{1}{2}$, $\frac{3}{4}$, and $\frac{1}{4}$ respectively. What is the probability
 that the problem will be solved?

b) For the curve $x = \cos t + t \sin t$, $y = \sin t - t \cos t$, find the tangential and normal (05)
 components of acceleration at any time t .

c) If $\vec{F} = (2xy + 3z^2)\hat{i} + (x^2 + 4yz)\hat{j} + (2y^2 + 6xz)\hat{k}$, evaluate $\int_C \vec{F} \cdot d\vec{r}$ where C is (05)
 the curve $x = t$, $y = t^2$, $z = t^3$ joining the points $(0, 0, 0)$ and $(1, 1, 1)$.

Q.6 a) Determine the equations of regression lines for the following data: (08)

x:	1	2	3	4	5	6	7	8	9
y:	9	8	10	12	11	13	14	16	15

And obtain an estimate of y for $x = 4.5$

b) The mean weight of 500 students is 63 kgs and the standard deviation is 8 kgs. (05)
 Assuming that the weights are normally distributed, find how many students
 weigh 52 kgs. The weights are recorded to the nearest kg.
 (Given: $z_1 = 1.44$, $A_1 = 0.4251$, $z_2 = 1.31$, $A_2 = 0.4049$)

Q.7 a) Find the directional derivative of the function $\phi = e^{2x-y-z}$ at $(1, 1, 1)$ in the (05)
 direction of the tangent to the curve
 $x = e^{-t}$, $y = 2 \sin t + 1$, $z = t - \cos t$ at $t = 0$.

b) Prove that : (08)

i) $\nabla \left(\frac{\vec{a} \cdot \vec{r}}{r^n} \right) = \frac{\vec{a}}{r^n} - \frac{n(\vec{a} \cdot \vec{r})}{r^{n+2}} \vec{r}$

ii) $\nabla^4 e^r = e^r + \frac{4}{r} e^r$

Q.8 a) Evaluate: $\iiint_S 2x^2 y dy dz - y^2 dz dx + 4xz^2 dx dy$ over the curved surface of the (06)
 cylinder $y^2 + z^2 = 9$, bounded by $x = 0$ and $x = 2$.

b) Verify stokes theorem when $\vec{F} = (2x - y)\hat{i} - yz^2\hat{j} - y^2z\hat{k}$, where S is the (07)
 upper half surface of the sphere $x^2 + y^2 + z^2 = 1$, and C is the boundary.