

F.Y.B.SC. SEM – II (CBCS - 2016 Course) : WINTER - 2018
SUBJECT : MATHEMATICS : INTEGRAL CALCULUS & DIFFERENTIAL EQUATIONS

Day : Thursday
Date : 25/10/2018

W-2018-0706

Time : 03.00 P.M. To 06.00 P.M
Max. Marks :60

N. B. :

- 1) All questions are **COMPULSORY**.
- 2) Figures to the right indicate **FULL** marks.

Q. 1 A) Select the correct alternatives of the following: (06)

i) $\int \frac{dx}{x^2+1} = \underline{\hspace{2cm}}$

- a) $\frac{1}{2} \tan^{-1} \left(\frac{x}{2} \right)$ b) $\tan^{-1} x$
c) $\tan^{-1} \left(\frac{x}{2} \right)$ d) $\frac{1}{2} \tan^{-1} x$

ii) $\int_0^{\pi/2} \sin^{10} x \, dx = \underline{\hspace{2cm}}$

- a) $\frac{63\pi}{512}$ b) $\frac{13\pi}{512}$ c) $\frac{\pi}{512}$ d) 0

iii) $\int_0^{\pi/2} \sin^6 x \cos^6 x \, dx = \underline{\hspace{2cm}}$

- a) $\frac{8\pi}{693}$ b) $\frac{1}{693}$ c) $\frac{8}{693}$ d) $\frac{8}{512}$

iv) $y = ax + b$ is an equation where a and b are arbitrary constants then its differential equation is $\underline{\hspace{2cm}}$

- a) $\frac{d^2y}{dx^2} + y = 0$ b) $\frac{dy}{dx} = 0$ c) $\frac{d^2y}{dx^2} = 0$ d) $\frac{d^2y}{dx^2} + xy = 0$

v) Substitution of $\frac{dy}{dx} = \frac{x+2y+1}{2x+4y+3}$ is $\underline{\hspace{2cm}}$

- a) $u = x + y$ b) $u = 2x + 2y$ c) $u = 2x + y$ d) $u = x + 2y$

vi) Solution of differential equation $ydx + xdy + 2zdz = 0$ is $\underline{\hspace{2cm}}$

- a) $xy + z^2 = c$ b) $2x + y = c$ c) $xyz = c$ d) $x + y = c$

B) Solve the following: (06)

i) State the formula for obtaining surface area of the curve $r = f(\theta)$

ii) Find order and degree of the differential equation: $L \frac{d^2q}{dt^2} + \frac{1}{c} q = E \sin \omega t$

iii) Find length of a curve $y = f(x)$ between $x = a$ and $x = b$.

iv) Define integrating factor of differential equation.

v) Define Bernoulli's differential equation.

vi) Evaluate $\int_0^{\pi/2} \sin^4 x \cos^4 x \, dx$.

(P.T.O)

Q.2 Attempt **ANY THREE** of the following: **(12)**

a) Define homogenous differential equation and explain the method of its solution.

b) Evaluate $\int \frac{(x-8)}{(2x-1)(x^3+x+3)} dx$

c) Evaluate $\int \frac{x^2+1}{x^4+1} dx$

d) Evaluate $\int \frac{x^2+x+1}{(x-1)^2(x-2)} dx$

Q.3 Attempt **ANY FOUR** of the following: **(12)**

a) Find circumference of circle $x^2 + y^2 = a^2$, by integration.

b) Solve : $(1+xy^2)dx + (1+x^2y)dy = 0$.

c) Solve : $(1+y^2)dx = (\tan^{-1} y - x)dy$.

d) Evaluate $\int_0^{\pi/6} \sin^6 3x dx$.

e) Evaluate $\int \tan^5 x dx$.

Q.4 Attempt **ANY TWO** of the following: **(12)**

a) Prove that the necessary and sufficient condition for the equation $Mdx + Ndy = 0$, where M and N are functions of x and y to be exact is that $\frac{\partial M}{\partial y} = \frac{\partial N}{\partial x}$.

b) Solve : $(x^2y - 2xy^2)dx - (x^3 - 3x^2y)dy = 0$.

c) Solve : $\frac{dy}{dx} - y \tan x + y^2 \sec^2 x = 0$

Q.5 Attempt **ANY TWO** of the following: **(12)**

a) Evaluate $\int \frac{dx}{a+b \sin x}$ if (i) $a^2 > b^2$ (ii) $a^2 < b^2$.

b) Find the length of the arc of the parabola $x^2 = 4ay$ measured from the vertex to one extremity of the latus rectum.

c) Evaluate the surface area of the solid generated by revolving the cycloid $x = a(\theta - \sin \theta)$, $y = a(1 - \cos \theta)$, about the line $y = 0$.

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