

**F.Y. B. SC. (COMPUTER SCIENCE) SEM – I (CBCS - 2016  
COURSE) : SUMMER - 2018  
SUBJECT: ALGEBRA-I**

**Day: Friday**  
**Date: 20/04/2018**

**S-2018-0795**

**Time: 11.00 A.M. TO 02.00 PM**  
**Max. Marks: 60**

**N.B.:**

- 1) All questions are **COMPULSORY**.
- 2) Non - programmable calculator is allowed.

**Q.1 A)** Select the correct alternative **(06)**

a) A relation R on set A is said to be antisymmetric if  $aRb$  and  $bRa \Rightarrow$  \_\_\_\_\_

- |                    |                 |
|--------------------|-----------------|
| i) $aRa$ and $bRb$ | ii) $a = b$     |
| iii) $a = -b$      | iv) $a = \pm b$ |

b) Fermat's theorem states if p is a prime number and  $a \in Z$  is not divisible by p then

- |                                  |                                 |
|----------------------------------|---------------------------------|
| i) $a^p \equiv 1 \pmod{p}$       | ii) $a^{p-5} \equiv 1 \pmod{p}$ |
| iii) $a^{p-3} \equiv 1 \pmod{p}$ | iv) $a^{p-1} \equiv 1 \pmod{p}$ |

c) In  $Z_3$   $(\overline{100}) =$

- |                     |                    |
|---------------------|--------------------|
| i) $\overline{0}$   | ii) $\overline{1}$ |
| iii) $\overline{2}$ | iv) None of these  |

d) Imaginary part of  $Z = \frac{i-i^2+i^3+i^4}{i^5+i^6+2} =$  \_\_\_\_\_

- |         |        |
|---------|--------|
| i) 1    | ii) 2  |
| iii) -1 | iv) -2 |

e) Polar form of complex number is \_\_\_\_\_

- |                                    |                                   |
|------------------------------------|-----------------------------------|
| i) $r(\cos\theta + i\sin\theta)$   | ii) $r(\sin\theta + i\cos\theta)$ |
| iii) $r(\cos\theta - i\sin\theta)$ | iv) $r(\sin\theta - i\cos\theta)$ |

f) Least common multiple of (121, 335) is \_\_\_\_\_

- |           |                   |
|-----------|-------------------|
| i) 3111   | ii) 4121          |
| iii) 4235 | iv) None of these |

g)  $M(R) = 0$  if and only if R is \_\_\_\_\_

- |                     |                |
|---------------------|----------------|
| i) Empty            | ii) Cannot say |
| iii) Sometime empty | iv) Non empty  |

**B)** Attempt all the following: **(06)**

- a) Define Equivalence class.
- b) Check whether the following function  $f(x) = -x + 2$  is onto or not.
- c) Write definition of least common multiple
- d) Prepare composition table for  $(Z_5, +_5)$ .
- e) Find real and imaginary part of  $Z = 3 - i$ .
- f) Find the Hamming distance between  $x = 1010101$  and  $y = 0011100$

**P.T.O.**

**Q.2** Attempt any **THREE** of the following: (12)

- a) Obtain remainder when  $8^{103}$  is divisible by 13 using Fermat's theorem.
- b) Prove that if  $c|ab$  and  $(b, c) = 1$  then  $c|a$ .
- c) Prove that if  $x, y, z \in B^m$  then
  - i)  $\delta(x, y) \geq 0$
  - ii)  $\delta(x, y) = 0$  iff  $x = y$
- d) Find modulus and argument of  $z = \frac{3-i}{2+i} + \frac{3+i}{2-i}$

**Q.3** Attempt any **FOUR** of the following: (12)

- a) Obtain  $f^{-1}$  of function  $f: R \rightarrow R$  such that  $f(x) = \frac{4x-3}{2}$ .
- b) Check whether the function  $f(n) = 2^n$  is one - one or not
- c) Find minimum distance  $d$  for the following code  $C = \{10000, 01010, 00001\}$  in  $Z_2^5$ .
- d) If  $Z_1$  and  $Z_2$  are complex numbers then show that  $|Z_1 + Z_2|^2 + |Z_1 - Z_2|^2 = 2|Z_1|^2 + 2|Z_2|^2$
- e) Obtain  $f \circ g$  if  $f: R \rightarrow R$  such that  $f(x) = x^2 - 1$  and  $g: R \rightarrow R$  such that  $g(x) = \frac{3x-4}{10}$

**Q.4** Attempt any **TWO** of the following: (12)

- a) Prove that  $R$  is equivalence relation, let  $R$  be a relation on  $Z$  defined by  $xRy$  if and only if  $3x + 4y$  is divisible by 7, for  $x, y, \in Z$
- b) Find transitive closure of  $R$  using Warshall's algorithm if  $R = \{(1, 3), (2,1), (2,4), (3,3), (4,1), (4, 2)\}$  be a relation on set  $A = \{1, 2, 3, 4\}$
- c) Solve  $x^4 - x^3 + x^2 - x + 1 = 0$  using Demoivre's theorem.

**Q5** Attempt any **TWO** of the following: (12)

- a) Find g.c.d of 4999 and 1109 and express the g.c.d. in the form  $4999m + 1109n$
- b) Prove that  $5^n - 1$  is divisible by for  $n \geq 1$  by using first principle of mathematical induction.
- c) Construct a decoding table with syndroms for a group code given by generator matrix  $G = \begin{bmatrix} 1 & 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 1 & 1 \end{bmatrix}$  use the table to decode the received word 10010.

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