

Day : Monday
Date : 03/06/2019

Time : 11.00 AM TO 02.00 PM
Max. Marks : 60

S-2019-3347

N.B.:

- 1) All questions are **COMPULSORY**.
- 2) Figures to the right indicate **FULL** marks.
- 3) Use of non programmable **CALCULATOR** is allowed.
- 4) Answer to both the sections should be written in **SAME** Answer book.

SECTION – I

- Q.1** The velocity $V(\text{km/min})$ of a moped which starts from rest is given at fixed intervals of time t (min) as follows: [10]

t	2	4	6	8	10	12	14	16	18	20
y	10	18	25	29	32	20	11	5	2	0

Estimate approximately the distance covered in 20 minutes.

OR

Use L – U decomposition method to solve the system of equations [10]

$$3x_1 + 2x_2 + 7x_3 = 4$$

$$2x_1 + 3x_2 + x_3 = 5$$

$$3x_1 + 4x_2 + x_3 = 7$$

- Q.2** i) The function $f(x)$ defined by $f(x) = \frac{a}{x} + bx$, $f(2) = 1$ has an extremum at $x = 2$. Determine a and b. [05]

- ii) The velocity of waves of wave-length λ on deep water is proportional to $\sqrt{\frac{a}{\lambda} + \frac{\lambda}{a}}$ where 'a' is certain constant. Prove that the velocity is minimum when $\lambda = a$. [05]

OR

For the function $f(x) = -0.1x^4 - 0.15x^3 - 0.5x^2 - 0.25x + 1.2$ approximate value of its derivative at $x = 0.5$. [10]

- i) Using Forward difference formula.
- ii) Using Backward difference formula.
- iii) Using Central difference formula.
- iv) Which of the above three is better approximation to the real answer?

- Q.3** Determine the response of damped vibrating system corresponding to. [10]

$$\frac{d^2y}{dt^2} + 4y = r(t), \text{ where } r(t) = \begin{cases} 1 & \text{if } 0 < t < 1 \\ 0 & \text{if } t > 1 \end{cases} \quad y(0) = 1, y'(0) = 0.$$

OR

Find the Fourier co-efficients of the periodic function $f(x)$ where [10]

$$f(x) = \begin{cases} -k & \text{if } -\pi < x < 0 \\ k & \text{if } 0 < x < \pi \end{cases} \quad \text{and } f(x+2\pi) = f(x)$$

P.T.O.

SECTION – II

Q.4 What is simulation? Discuss data manipulation and data exchange of structures, role in simulation. [10]

OR

Explain metropolis algorithm using the Monte Carlo Markov chains. [10]

Q.5 Write a note on Monte Carlo methods using the following points : [10]

- i) The need for Monte Carlo methods
- ii) Monte Carlo method in mathematics.

OR

Discuss finite difference methods with reference to truncation error, single and multi-step schemes. [10]

Q.6 Discuss Nano-design and Nano CAD. [10]

OR

Write a short note on nano-optics. [10]

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